

AS Level Mathematics A

H230/02 Pure Mathematics and Mechanics

Question Set 6

- 1 A particle is in equilibrium under the action of the following three forces:

$(2p\mathbf{i} - 4\mathbf{j})\text{ N}$, $(-3q\mathbf{i} + 5p\mathbf{j})\text{ N}$ and $(-13\mathbf{i} - 6\mathbf{j})\text{ N}$.

Find the values of p and q .

[3]

$$F_1 + F_2 + F_3 = 0$$

$$2p - 3q - 13 = 0$$

$$-4 + 5p - 6 = 0$$

$$p = 2 \quad q = -3$$

- 2 A crane lifts a car vertically. The car is inside a crate which is raised by the crane by means of a strong cable. The cable can withstand a maximum tension of 9500 N without breaking. The crate has a mass of 55 kg and the car has a mass of 830 kg.

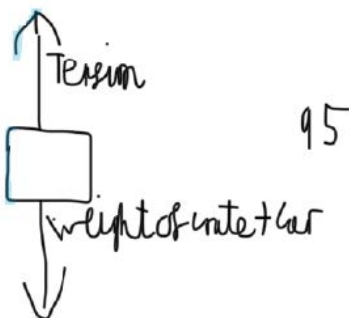
- (a) Find the maximum acceleration with which the crate and car can be raised.

[2]

$$9500 - 55g - 830g = 885a \quad a = 0.934 \text{ ms}^{-2}$$

- (b) Show on a clearly labelled diagram the forces acting on the crate while it is in motion.

[1]



- (c) Determine the magnitude of the reaction force between the crate and the car when they are ascending with maximum acceleration.

[3]

$$R - 830g = 830a \quad R = 8910 \text{ N}$$

- 3 A particle P is moving in a straight line. At time t seconds P has velocity $v \text{ ms}^{-1}$ where $v = (2t+1)(3-t)$.

$$v = -2t^2 + 5t + 3$$

$$a = -4t + 5$$

- (a) Find the deceleration of P when $t = 4$.

[2]

$$= 9 \text{ m/s}^2$$

- (b) State the positive value of t for which P is instantaneously at rest.

[1]

$$v = 0 \quad t = 3$$

(c) Find the total distance that P travels between times $t = 0$ and $t = 4$.

[3]

$$s = \int_0^4 v dt = \int_0^4 (-2t^2 + 5t + 3) dt = \left[-\frac{2}{3}t^3 + \frac{5}{2}t^2 + 3t \right]_0^4 = \left(-\frac{2}{3} \times 64 + \frac{5}{2} \times 16 + 3 \times 4 \right) - 0 = \frac{28}{3}$$

4 A car starts from rest at a set of traffic lights and moves along a straight road with constant acceleration 4 ms^{-2} . A motorcycle, travelling parallel to the car with constant speed 16 ms^{-1} , passes the same traffic lights exactly 1.5 seconds after the car starts to move. The time after the car starts to move is denoted by t seconds.

for bike $s = 16(t - 1.5)$

(a) Determine the two values of t at which the car and motorcycle are the same distance from the traffic lights. [6]

Car

$$s =$$

$$v = 0 \quad s = 2t^2$$

$$v =$$

$$a = 4$$

$$T = t$$

$$s = ut + \frac{at^2}{2}$$

$$16t - 24 = 2t^2 \quad t^2 - 8t + 12 = 0 \quad \begin{matrix} t = 2 \\ t = 6 \end{matrix} \quad (s_{\text{bike}} = s_{\text{car}})$$

(b) Describe the relative positions of the car and the motorcycle when $t_1 < t < t_2$. [1]

Motor bike in front of car

(c) Determine the maximum distance between the car and the motorcycle when $t_1 < t < t_2$. [3]

$$\frac{ds}{dt} = 2t^2 - 16t - 24 = 0 \quad \downarrow \quad \begin{matrix} s \text{ for car at } t=4 = 32 \\ s \text{ for bike at } t=4 = 40 \end{matrix} \quad \therefore \text{max distance between} = 8 \text{ m}$$

Total Marks for Question Set 6: 25